

## 6902 Three Squares

A square is called axis-parallel if its sides are vertical or horizontal, and two squares are said to be congruent if their side lengths are equal. You are given a set  $P$  of  $n$  points in the plane. Any real number  $x \geq 0$  is called *3SQ-sufficient* for  $P$  if there exist three congruent axis-parallel squares of side length  $x$  such that the union of the three squares contains all points in the set  $P$ . If a square has side length zero, it is degenerated to a point, so you can consider a point itself as a square of side length zero. Your program is to find the smallest 3SQsufficient number for a given input set  $P$  of points.

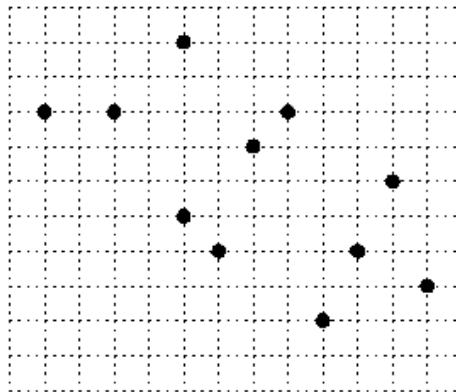
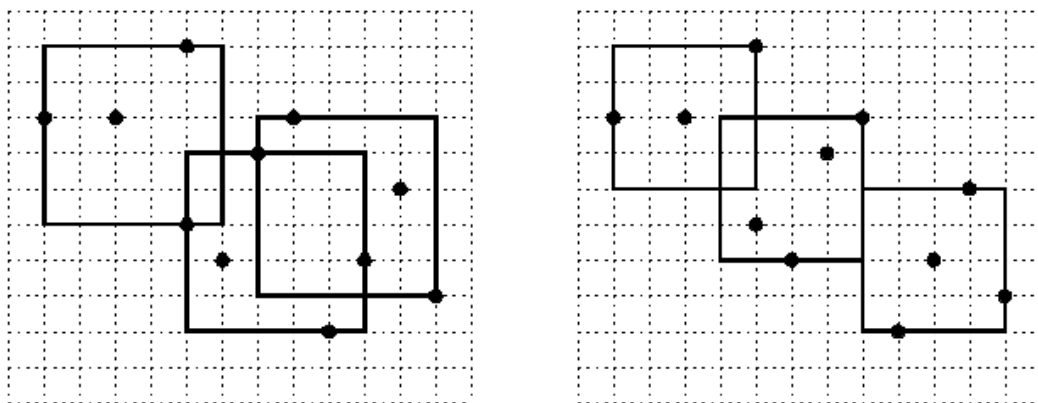


Figure 1. 11 points in the plane

For example, let  $P$  be the set of 11 points in the plane as shown in Figure 1. Then, one can find three congruent axis-parallel squares of side length 5 whose union contains all these 11 points in the set  $P$ , as shown in Figure 2(a). This means that number 5 is 3SQ-sufficient for this set  $P$  of 11 points. Notice that points on the boundary of a square are considered to be contained in the square.



(a) (b)  
Figure 2. Two numbers 5 and 4 are 3SQ-sufficient

You can find an even smaller 3SQ-sufficient number for this case; there exist three axis-parallel squares of side length 4 whose union contains all the 11 points as illustrated in Figure 2(b). More effort to find a further smaller 3SQ-sufficient number will be however worthless because number 4 is in fact the smallest 3SQsufficient number for this set  $P$ . Therefore, if these 11 points of Figure 1 are given as input of your program, then your program must output 4 as the answer.

## Input

Your program is to read from standard input. The input consists of  $T$  test cases. The number of test cases  $T$  is given in the first line of the input. Each test case starts with a line containing an integer,  $n$  ( $1 \leq n \leq 100,000$ ), where  $n$  is the number of points in the data set  $P$ . In the following  $n$  lines, each of the  $n$  points in  $P$  is given line by line. Each point is represented by two numbers separated by a single space, which are the  $x$ -coordinate and the  $y$ -coordinate of the point, respectively. Each coordinate is given as an integer between  $-1,000,000,000$  and  $1,000,000,000$ , inclusively. Note that there may be two or more points having the same coordinates in the input data set  $P$ .

## Output

Your program is to write to standard output. Print exactly one line for each test case. The line should contain an integer representing the smallest 3SQ-sufficient integer for a given input set  $P$  of points.

The following shows sample input and output for three test cases.

## Sample Input

```
3
5
1 0
0 1
5 2
2 3
3 2
11
1 8
3 8
5 5
5 10
6 4
7 7
8 8
9 2
11 6
12 3
10 4
4
1 1
2 8
-21 45
1 1
```

## Sample Output

```
1
4
0
```