

## 6303 Species Evolution

If a group of genes remain physically close to each other in multiple genomes, often called *gene clusters*, then the genes may be either historically or functionally related. Thus, the study of gene clusters is important for the understanding of evolution, since genomes evolved from a common ancestor tend to share the same varieties of gene clusters.

There are many gene cluster models. Dr. Lee uses the following approach to evaluate the quality of a given model. First, he finds a sequence of  $n$  species  $(S_1, S_2, \dots, S_n)$ , where each  $S_i$ ,  $2 \leq i \leq n$ , is evolved from  $S_{i-1}$ . Let  $k$  be a positive integer. Define  $[0, k]$  to be an integer set ranging from 0 to  $k$ . Based upon the given gene cluster model, Dr. Lee computes a sequence of numbers  $A = (a_1, a_2, \dots, a_n)$ , where each  $a_i$ ,  $1 \leq i \leq n$ , is an integer in  $[0, k]$  indicating the score of similarity between  $S_i$  and  $S_n$ . Of course,  $a_n = k$ . Dr. Lee believes that a perfect gene cluster model should satisfy the following two properties:

- P1.** The sequence  $A$  is digressing (i.e.,  $a_1 \leq a_2 \leq \dots \leq a_n$ ). This property indicates that  $S_n$  is more similar to  $S_i$  than to  $S_{i-1}$ ,  $2 \leq i \leq n$ .
- P2.** For  $2 \leq i \leq n$ , the difference between  $a_{i-1}$  and  $a_i$  is bounded by some threshold  $\delta$  (i.e.,  $a_i - a_{i-1} \leq \delta$ ). This property indicates that  $S_i$  should not deviate far from  $S_{i-1}$ , since  $S_i$  is evolved from  $S_{i-1}$ .

In practice, the sequence  $A$  may not satisfy properties P1 and P2. Let  $R^n$  be the set of all possible sequences of  $n$  integers that satisfy properties P1 and P2. Dr. Lee defines the *distance* between  $A$  and a sequence  $X = (x_1, x_2, \dots, x_n) \in R^n$  to be  $d(A, X) = \sum_{1 \leq i \leq n} (x_i - a_i)^2$ . (You may consider  $d(A, X)$  as the total cost of modifying each  $a_i$  to  $x_i$ ,  $1 \leq i \leq n$ .) In addition, he defines the *inaccuracy* of the given gene cluster model to be  $\varepsilon(A) = \min_{X \in R^n} \{d(A, X)\}$ . In other words, he defines the inaccuracy to be the minimum cost of modifying  $A$  into a sequence (of  $n$  integers) that satisfies properties P1 and P2.

Consider an example of  $n = 4$ ,  $k = 10000$ ,  $\delta = 3000$ , and  $A = (5000, 2000, 6000, 10000)$ . Let  $B = (5000, 7000, 10000, 12000)$ ,  $C = (3500, 3500, 6500, 9500)$ ,  $D = (5000, 4000, 6000, 8000)$ , and  $E = (5000, 5500, 6000, 10000)$ . Both  $B$  and  $C$  are in the set  $R^4$ . However,  $D$  and  $E$  are not, since they do not satisfy P1 and P2, respectively. We have  $d(A, B) = (5000 - 5000)^2 + (7000 - 2000)^2 + (10000 - 6000)^2 + (12000 - 10000)^2 = 45000000$  and  $d(A, C) = (3500 - 5000)^2 + (3500 - 2000)^2 + (6500 - 6000)^2 + (9500 - 10000)^2 = 5000000$ . In this example,  $C$  has the minimum distance from  $A$  among all sequences in  $R^4$ . Thus,  $\varepsilon(A) = 5000000$ .

Please write a program to compute  $\varepsilon(A)$ .

### Input

There are at most 10 test cases. Each case consists of two lines. The first line contains the integer  $n$  ( $1 \leq n \leq 100$ ), the integer  $k$  ( $10000 \leq k \leq 50000$ ), and the integer  $\delta$  ( $0 \leq \delta \leq 5000$ ). The second line contains the sequence  $A = (a_1, a_2, \dots, a_n)$ , where  $a_i \in [0, k]$  for  $1 \leq i \leq n - 1$  and  $a_n = k$ . The last test case will be followed by a line containing a single zero.

### Output

For each test case, output one line for  $\varepsilon(A)$ .

**Sample Input**

```
4 10000 3000
5000 2000 6000 10000
3 10000 2000
8200 5900 10000
0
```

**Sample Output**

```
5000000
3246667
```