

## 5809 Binary Matrix

You are given an  $M \times N$  binary matrix. By  $M \times N$  matrix we mean a matrix having  $M$  rows and  $N$  columns and by binary matrix we mean each of the  $M \times N$  elements is a binary value, either '0' or '1'. In addition, this matrix wraps both in horizontally and vertically. So  $i$ -th row is adjacent to  $(i + 1)$ -th row for all  $1 \leq i < M$  and  $M$ -th row is adjacent to 1st row. Similarly,  $i$ -th column is adjacent to  $(i + 1)$ -th column for all  $1 \leq i < N$  and  $N$ -th column is adjacent to 1st column. Obviously row  $a$  is adjacent to row  $b$  implies that row  $b$  is adjacent to row  $a$ , and same thing is true for columns. Now, two cells of this matrix are adjacent if they are in the same row and their columns are adjacent, or they are in the same column and their rows are adjacent. So for a  $3 \times 5$  matrix, cell  $(2, 3)$  has 4 adjacent cells  $(1, 3)$ ,  $(2, 2)$ ,  $(2, 4)$ ,  $(3, 3)$  and cell  $(3, 5)$  has 4 adjacent cells  $(2, 5)$ ,  $(3, 4)$ ,  $(3, 1)$ ,  $(1, 5)$ . Note that, by cell  $(i, j)$  we mean the cell of  $i$ -th row and  $j$ -th column.



You are only allowed to swap the values of any two adjacent cells of the matrix. Your task is to transform the matrix in such a way so that, each of the rows has same number of '1's and each of the columns has same number of '1's. If it is possible print 'both' and also print the minimum number of swaps required. If it is not possible try to make every row has equal number of 1s. If it is possible print 'row' and also print the minimum number of swaps required. If it is also not possible try to make every column has equal number of 1s. If it is possible print 'column' and also print the minimum number of swaps required. If none of these possible you have to print 'impossible'.

### Input

The input starts with an integer  $T$  ( $T \leq 10$ ), number of test cases.

Each case starts with two integers  $M$  and  $N$  ( $2 \leq M, N \leq 1000$ ), number of rows and columns of the matrix. Next  $M$  lines denotes  $M$  rows of the matrix.  $j$ -th character of the  $i$ -th line denotes the value of cell  $(i, j)$  of the matrix.

### Output

For each case, output a single line. If task is impossible to complete, output 'Case #: impossible' otherwise print 'Case #: *solution\_type* *min\_swap*' without quotes, here # will be replaced by the case number, *solution\_type* will be replaced by the type of solution found as described above it will be one of these three 'both', 'row', 'column' without quotes and *min\_swap* will be replaced by the minimum number of swaps required to complete the task. Please note that value of *min\_swap* can be zero.

See the sample input and output for exact format.

### Explanation of sample input and output:

Case 1. The initial matrix is:

```
001
111
```

If we swap values of cell (1, 1) and cell (2, 1), the matrix will become

```
101
011
```

Now each row has two '1's and we found the solution.

**Case 2.** The initial matrix is:

```
001
011
000
```

If we swap the values of cell (2, 1) and cell (2, 3) (Considering the matrix wraps), the matrix will become

```
001
110
000
```

If we swap the values of cell (2, 1) and cell (3, 1), the matrix will become.

```
001
010
100
```

Now each row has one 1 and each column has one 1 and we got our solution.

### Sample Input

```
2
2 3
001
111
3 3
001
011
000
```

### Sample Output

```
Case 1: row 1
Case 2: both 2
```