

## 2872 Fully Diversified Sequences of Sets

Given a positive integer  $n$ , let  $N$  be the set of integers from 1 to  $n$ . A finite sequence  $A_1, \dots, A_k$  of subsets of  $N$  is *fully diversified* if:

- Each subset  $A_i$  has an even number of elements.
- For each element  $m$  in  $N$ , there are exactly  $m$  sets  $A_i$  in the sequence with  $m$  as a member.

For example, the sequence of subsets  $\{1,3\}, \{2,3\}, \{2,3\}$  is a fully diversified sequence of subsets of  $\{1,2,3\}$ . (Note that subsets in the sequence may be the same.)

A fully diversified sequence of subsets of  $N$  is **minimal** if no other fully diversified sequence of subsets of  $N$  has a smaller sequence count. The example above is minimal since the element 3 must occur in 3 different sets.

Write a program, which, given an integer  $n$ , determines whether there is a fully diversified sequence of subsets of the corresponding set  $N$  and, if there is a fully diversified sequence, finds a minimal fully diversified sequence of subsets of  $N$ .

### Input

The input will be a sequence of positive integers  $n$ , one per line followed by a zero (0) (on another line) indicating the end of the input.

### Output

If there is no fully diversified sequence of subsets of the corresponding set  $N$ , output a '0' on one line followed by a blank line.

If there is a fully diversified sequence of subsets of the corresponding set  $N$ , output the number of sets in your minimal sequence on one line, followed by the sets, one per line, followed by a blank line.

The elements of each set should be output in increasing order with a single space between numbers. The sets of sequences should be output in lexicographical order.

**There may be many possible solutions to each problem.**

### Sample Input

```
8
9
11
17
0
```

### Sample Output

```
8
1 3 5 6 7 8
2 4 5 6 7 8
2 4 5 6 7 8
3 4 5 6 7 8
6 8
```

7 8

7 8

0

11

1 5 7 8 9 11

2 5 7 8 10 11

2 5 7 8 10 11

3 5 7 9 10 11

3 6 7 9 10 11

3 6 7 9 10 11

4 6 8 9 10 11

4 6 8 9 10 11

4 6 8 9 10 11

4 6 8 9 10 11

5 7 8 9 10 11

0